# MATH-1380: MATHEMATICS FOR ELEMENTARY AND MIDDLE SCHOOL TEACHERS II

# **Cuyahoga Community College**

Viewing: MATH-1380: Mathematics for Elementary and Middle School Teachers II

**Board of Trustees:** 

March 2023

**Academic Term:** 

Fall 2023

**Subject Code** 

MATH - Mathematics

**Course Number:** 

1380

Title:

Mathematics for Elementary and Middle School Teachers II

#### **Catalog Description:**

Second of two-semester sequence designed for elementary and middle school education majors. Emphasis on understanding ideas and concepts. Includes statistics, probability, measurement, geometric shapes, Euclidean geometry, coordinate geometry, transformational geometry, problem-solving strategies, and historical topics. Highlights applications to classroom, projects, and use of current technology, including scientific/graphing calculators and computers.

# Credit Hour(s):

4

#### Lecture Hour(s):

4

# Requisites

#### **Prerequisite and Corequisite**

MATH-1370 Mathematics for Elementary and Middle School Teachers I, or departmental approval: equivalent coursework.

# Outcomes

# Course Outcome(s):

Collect, organize, display, analyze, and interpret data.

#### **Essential Learning Outcome Mapping:**

Quantitative Reasoning: Analyze problems, including real-world scenarios, through the application of mathematical and numerical concepts and skills, including the interpretation of data, tables, charts, or graphs.

#### Objective(s):

- a. Describe the population and sample in a survey.
- b. Use proportional reasoning to extrapolate information from a sample.
- c. Describe the attributes of categorical data as compared to numerical data.
- d. Describe bias in a survey.
- e. Construct a line plot and a stem and leaf plot.
- f. Construct a line graph and a circle graph.
- g. Plot information in a scatterplot and draw a regression line.
- h. Calculate measures of center and dispersion and interpret distributions of various shapes.
- i. Find the mean, mode and median for a collection of numbers.
- j. Construct a box and whisker plot.
- k. Describe the properties of the normal distribution.
- I. Calculate the variance.

- m. Find the standard deviation for data.
- n. Calculate the z-scores.

#### Course Outcome(s):

Compute probabilities for simple and complex experiments.

#### **Essential Learning Outcome Mapping:**

Quantitative Reasoning: Analyze problems, including real-world scenarios, through the application of mathematical and numerical concepts and skills, including the interpretation of data, tables, charts, or graphs.

#### Objective(s):

- a. Describe the sample space for an experiment.
- b. Calculate experimental probability.
- c. Find the theoretical probabilities of the outcomes.
- d. Use Pascal's Triangle to find probabilities.
- e. Evaluate expressions involving factorials.
- f. Calculate permutations and combinations.
- g. Find the expected value of an experiment.
- h. Find the odds in favor and against an event.
- i. Find the probability given the odds.
- j. Find compound and conditional probabilities.

#### Course Outcome(s):

Describe and analyze two-dimensional and three-dimensional shapes.

#### **Essential Learning Outcome Mapping:**

Quantitative Reasoning: Analyze problems, including real-world scenarios, through the application of mathematical and numerical concepts and skills, including the interpretation of data, tables, charts, or graphs.

#### Objective(s):

- a. Find, sort, and construct two-dimensional and three-dimensional shapes, including, but not limited to, rectangle, triangle, parallelograms, prisms.
- b. Identify the characteristics of two-dimensional and three-dimensional shapes.
- c. Complete basic geometric proofs.

# Course Outcome(s):

Solve problems involving measurement, conversion of measurements, area, and volume.

# **Essential Learning Outcome Mapping:**

Quantitative Reasoning: Analyze problems, including real-world scenarios, through the application of mathematical and numerical concepts and skills, including the interpretation of data, tables, charts, or graphs.

#### Objective(s):

- a. Solve problems involving measurement, conversion of measurements, area, and volume.
- b. Explain the central role of units in assigning values to measurements.
- c. Compute and verify ratios using U.S. customary units and metric units.
- d. Solve proportions involving measurements.
- e. Relate the processes of multiplication and division to the role of comparative sizing of units in unit conversion.
- f. Use dimensional analysis and unit rates to convert units and to solve problems involving measurement.
- g. Find the length of a line segment and represent it as a number of unit lengths.
- h. Find the perimeter and area of various figures and represent them as a number of unit lengths and unit areas.
- i. Apply the Pythagorean theorem to applications of measurement.
- j. Find the surface area and volume of three-dimensional figures and represent them as a number of unit squares and unit cubes.

- k. Define the distinction between precision and accuracy.
- I. Compare and contrast appropriate applications of precision and rounding.

#### Course Outcome(s):

Draw, construct, and describe geometrical figures and understand congruence and similarity.

#### **Essential Learning Outcome Mapping:**

Quantitative Reasoning: Analyze problems, including real-world scenarios, through the application of mathematical and numerical concepts and skills, including the interpretation of data, tables, charts, or graphs.

#### Objective(s):

- a. Complete proofs using properties of congruence.
- b. Solve proportions involving similarity.
- c. Use similarity properties to find missing lengths in application problems.
- d. Complete constructions using compass and straightedge.
- e. Describe geometric shapes based on relationships of sides and angles.
- f. Use Euclidean geometry to solve applied problems.
- g. Complete proofs using Euclidean geometry along with compass and straightedge.

# Course Outcome(s):

Use coordinate geometry to represent and examine the properties of geometric shapes.

#### **Essential Learning Outcome Mapping:**

Quantitative Reasoning: Analyze problems, including real-world scenarios, through the application of mathematical and numerical concepts and skills, including the interpretation of data, tables, charts, or graphs.

#### Objective(s):

- a. Explain how the Pythagorean Theorem pertains to the distance formula.
- b. Use the Pythagorean Theorem and the distance formula to show three points are collinear.
- c. Find the midpoint of a line segment.
- d. Calculate the slopes of lines.
- e. Describe the relationship between slope and linear variation.
- f. Describe the relationship between variation, indirect variation, and linear variation.
- g. Find the equations of lines.
- h. Graph equations and find their simultaneous solutions.
- i. Illustrate the use of triangles to obtain the formulas for circumference and area of a circle.
- j. Use coordinate geometry to solve applied problems.
- k. Complete proofs using coordinate geometry.

# Course Outcome(s):

Describe and examine the sizes, positions, and orientations of shapes under transformations.

# **Essential Learning Outcome Mapping:**

Quantitative Reasoning: Analyze problems, including real-world scenarios, through the application of mathematical and numerical concepts and skills, including the interpretation of data, tables, charts, or graphs.

#### Objective(s):

- a. Find the measure of directed angles.
- b. Find the image under various transformation, including, but not limited to, rotations, reflections, glide translations, and dilations.
- c. Describe the preservation of congruence and similarity under various transformations.
- d. Use transformations to solve applied problems.
- e. Complete proofs using transformational geometry.

# Course Outcome(s):

Apply a variety of strategies to solve problems that arise in mathematics and other fields.

#### **Essential Learning Outcome Mapping:**

Quantitative Reasoning: Analyze problems, including real-world scenarios, through the application of mathematical and numerical concepts and skills, including the interpretation of data, tables, charts, or graphs.

#### Objective(s):

- a. Use and apply strategies of look for a formula, do a simulation, and use a model.
- b. Use and apply strategies of use dimensional analysis and identify sub goals.
- c. Use and apply strategies of use coordinates and use symmetry.

#### Methods of Evaluation:

- a. Periodic exams
- b. Quizzes
- c. Homework
- d. Cooperative group work
- e. Project
- f. Portfolio
- g. Calculator/computer application problems
- h. Comprehensive final exam

# **Course Content Outline:**

- a. Statistics
  - i. Organizing and displaying data
  - ii. Charts and graphs
  - iii. Measuring central tendency
  - iv. Measuring dispersion
  - v. Distributions
  - vi. Misleading graphs
  - vii. Sampling bias
- b. Probability
  - i. Simple experiments
  - ii. Computing probability in simple experiments
  - iii. Tree diagrams and counting techniques
  - iv. Probability tree diagrams
  - v. Permutations
  - vi. Combinations
  - vii. Pascal's triangle and combinations
  - viii. Probability using counting techniques
  - ix. Simulations
  - x. Expected value
  - xi. Odds
  - xii. Conditional probability
- c. Geometric shapes
  - i. Recognizing geometric shapes
  - ii. Analyzing geometric shapes
  - iii. Symmetry
  - iv. Relationships between geometric shapes
  - v. Triangles and quadrilaterals
  - vi. Points and lines in a plane
  - vii. Angles
  - viii. Angles associated with parallel lines
  - ix. Regular polygons
  - x. Angle measures in regular polygons
  - xi. Tessellations

- xii. Circles
- xiii. Planes, skew lines, and dihedral angles
- xiv. Polyhedral
- xv. Curved shapes in three-dimensions
- d. Measurement
  - i. Nonstandard units
  - ii. Standard units in English and metric
  - iii. Dimensional analysis
  - iv. Length
  - v. Area
  - vi. Pythagorean theorem
  - vii. Surface area
  - viii. Volume
- e. Euclidean geometry
  - i. Triangle congruence
  - ii. Triangle similarity
  - iii. Indirect measurement
  - iv. Fractals and self-similarity
  - v. Constructions using compass and straightedge
  - vi. Geometric problem solving
- f. Coordinate geometry
  - i. Distance
  - ii. Slope
  - iii. Equations of lines
  - iv. Simultaneous equations
  - v. Equations of circles
  - vi. Geometric problem solving
- g. Transformational geometry
  - i. Isometries
  - ii. Symmetry
  - iii. Escher-type patterns
  - iv. Similitudes
  - v. Congruence
  - vi. Similarity
  - vii. Geometric problem solving
- h. Problem solving strategies
  - i. Look for a formula
  - ii. Do a simulation
  - iii. Use a model
  - iv. Use dimensional analysis
  - v. Identify sub goals
  - vi. Use coordinates
  - vii. Use symmetry

# Resources

Bassarear, Tom and Meg Moss. Mathematics for Elementary School Teachers. 7th ed. Cengage Learning, 2020.

Bennett, Albert B., Ted Nelson, and Laurie J. Burton. *Mathematics for Elementary School Teachers: A Conceptual Approach*. 10th ed. McGraw Hill, 2015.

Billstein, Rick, Shlomo Libeskind, and Johnny W. Lott. *A Problem Solving Approach to Mathematics for Elementary School Teachers*. 13th ed. Pearson Education, Inc., 2020.

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Musser, Gary L., William F. Burger, and Blake E. Peterson. *Mathematics for Elementary School Teachers: A Contemporary Approach.* 10th ed. John Wiley & Sons, Inc., 2014.

O'Daffer, Phares, Randall Charles, Thomas Cooney, John Dossey, and Jane Schielack. *Mathematics for Elementary School Teachers*. 4th ed. Pearson Education, Inc., 2008.

"Ohio Journal of School Mathematics"

"Principles and Standards for School Mathematics"

"Teaching Children Mathematics; Mathematics Teaching in the Middle School; Mathematics Teacher; and Journal for Research in Mathematics Education"

#### **Resources Other**

Software:

The Geometer's Sketchpad. McGraw Hill Education, 2014.

Website:

National Library of Virtual Manipulatives. nlvm.usu.edu. Utah State University.

# Instructional Services

# **OAN Number:**

Ohio Transfer 36 TMMSL

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